

Stanford CS224W: Machine Learning with Graphs

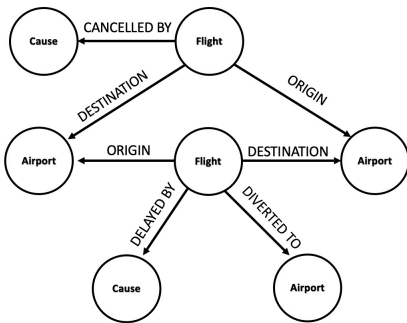
CS224W: Machine Learning with Graphs
Jure Leskovec, Stanford University
<http://cs224w.stanford.edu>



Why Graphs?

Graphs are a general language for describing and analyzing entities with relations/interactions

Many Types of Data are Graphs (1)

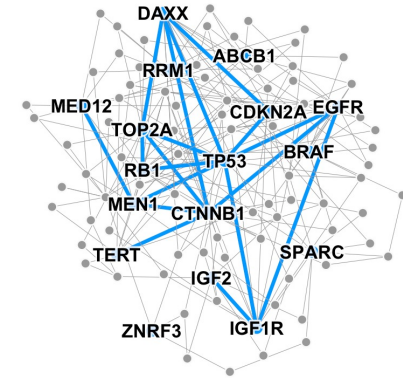


Event Graphs



Image credit: [SalientNetworks](#)

Computer Networks



Disease Pathways

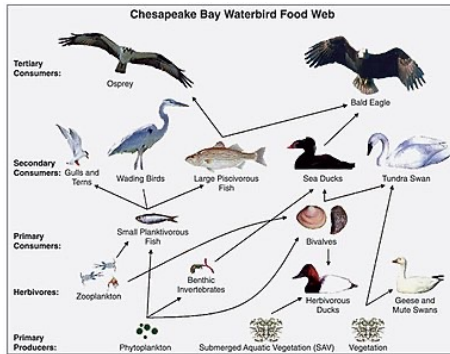


Image credit: [Wikipedia](#)

Food Webs



Image credit: [Pinterest](#)

Particle Networks

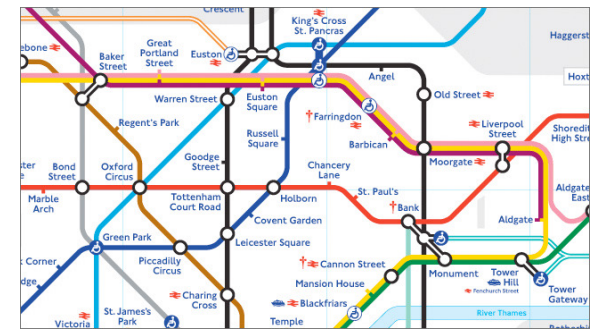


Image credit: [visitlondon.com](#)

Underground Networks

Many Types of Data are Graphs (2)



Image credit: [Medium](#)

Social Networks

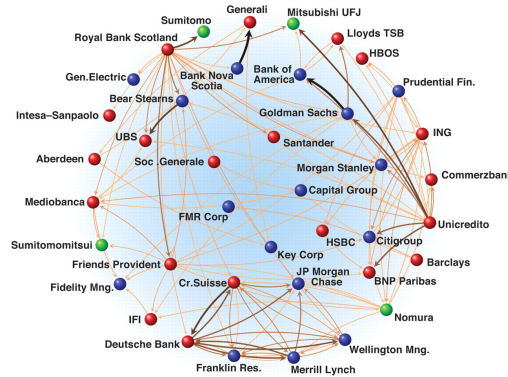


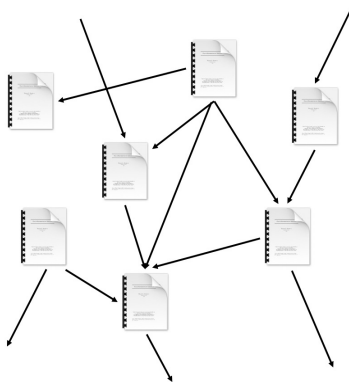
Image credit: [Science](#)

Economic Networks



Image credit: [Lumen Learning](#)

Communication Networks



Citation Networks



Image credit: [Missoula Current News](#)

Internet

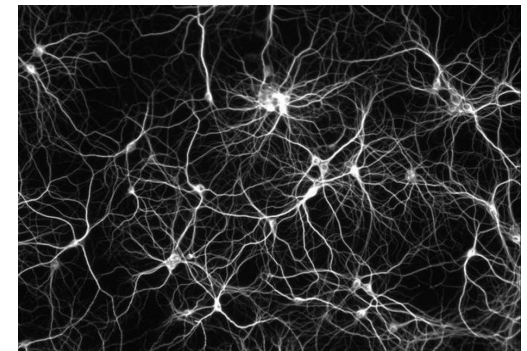


Image credit: [The Conversation](#)

Networks of Neurons

Many Types of Data are Graphs (3)

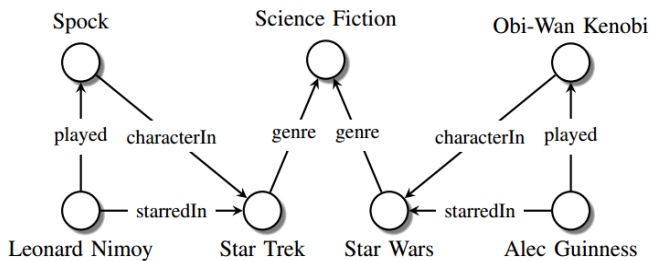


Image credit: [Maximilian Nickel et al](#)

Knowledge Graphs

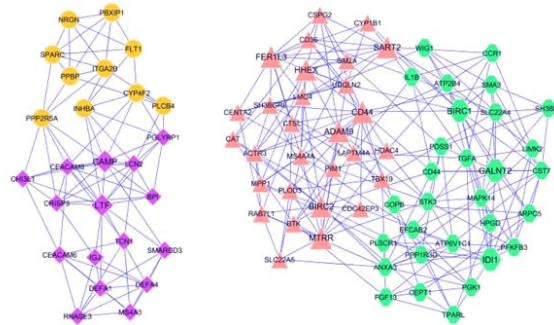


Image credit: [ese.wustl.edu](#)

Regulatory Networks

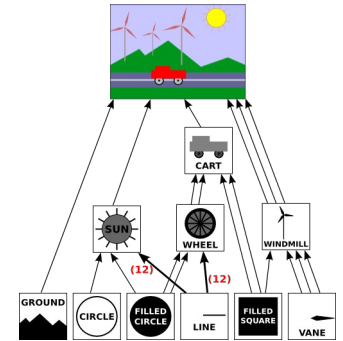


Image credit: [math.hws.edu](#)

Scene Graphs

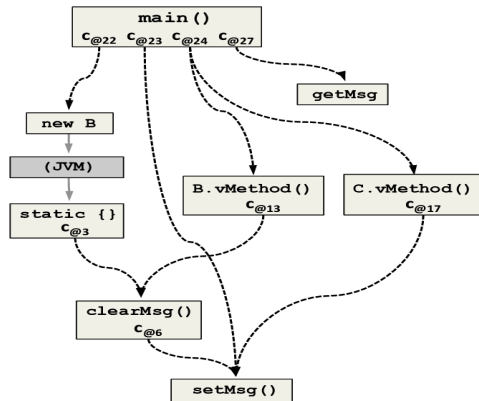


Image credit: [ResearchGate](#)

Code Graphs

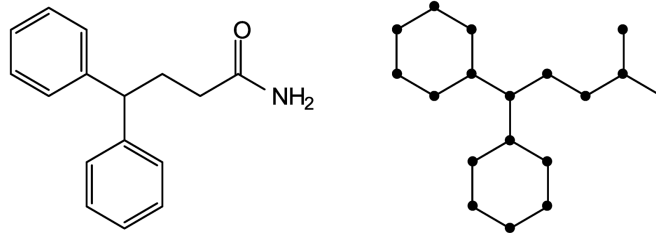


Image credit: [MDPI](#)

Molecules

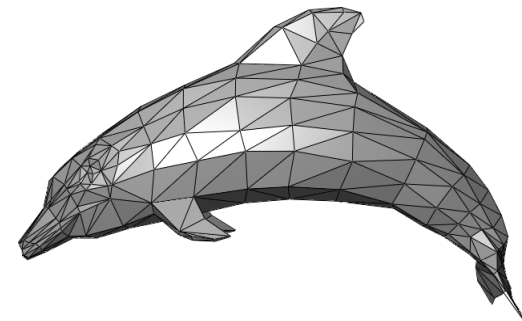
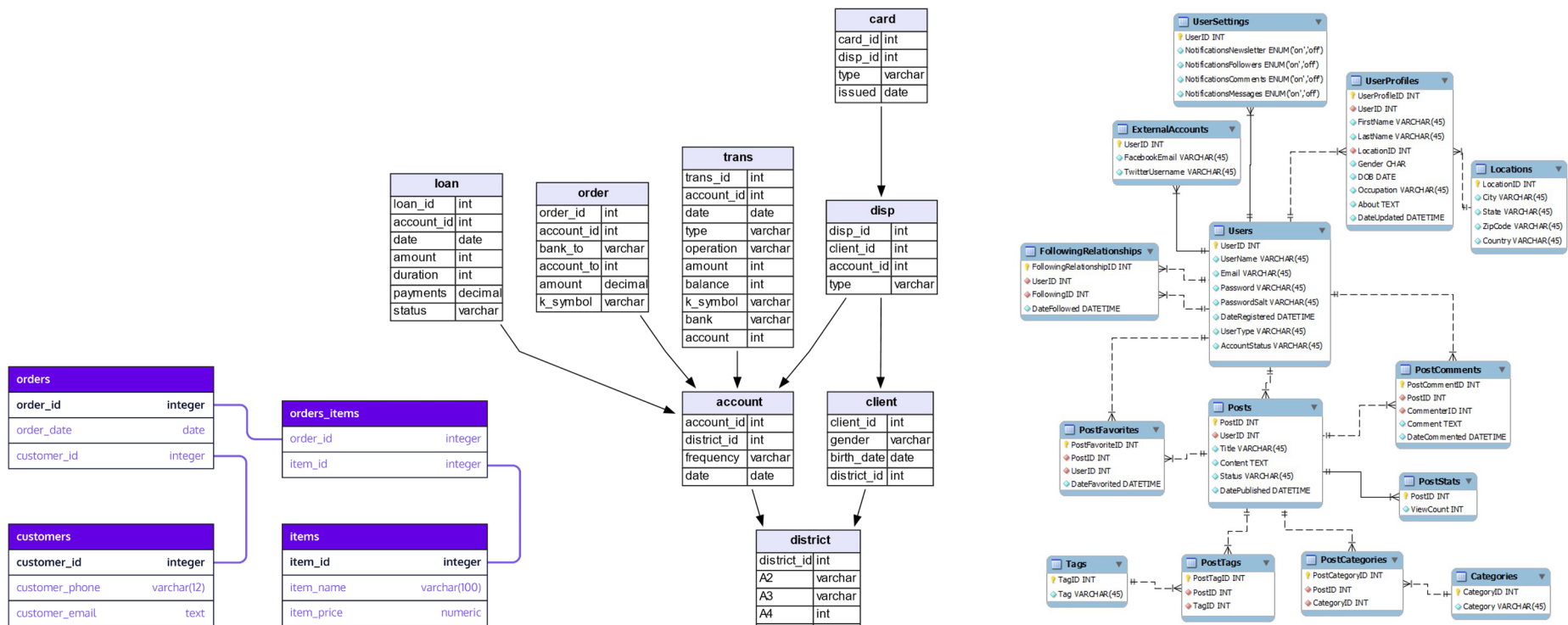


Image credit: [Wikipedia](#)

3D Shapes

Databases are Graphs!

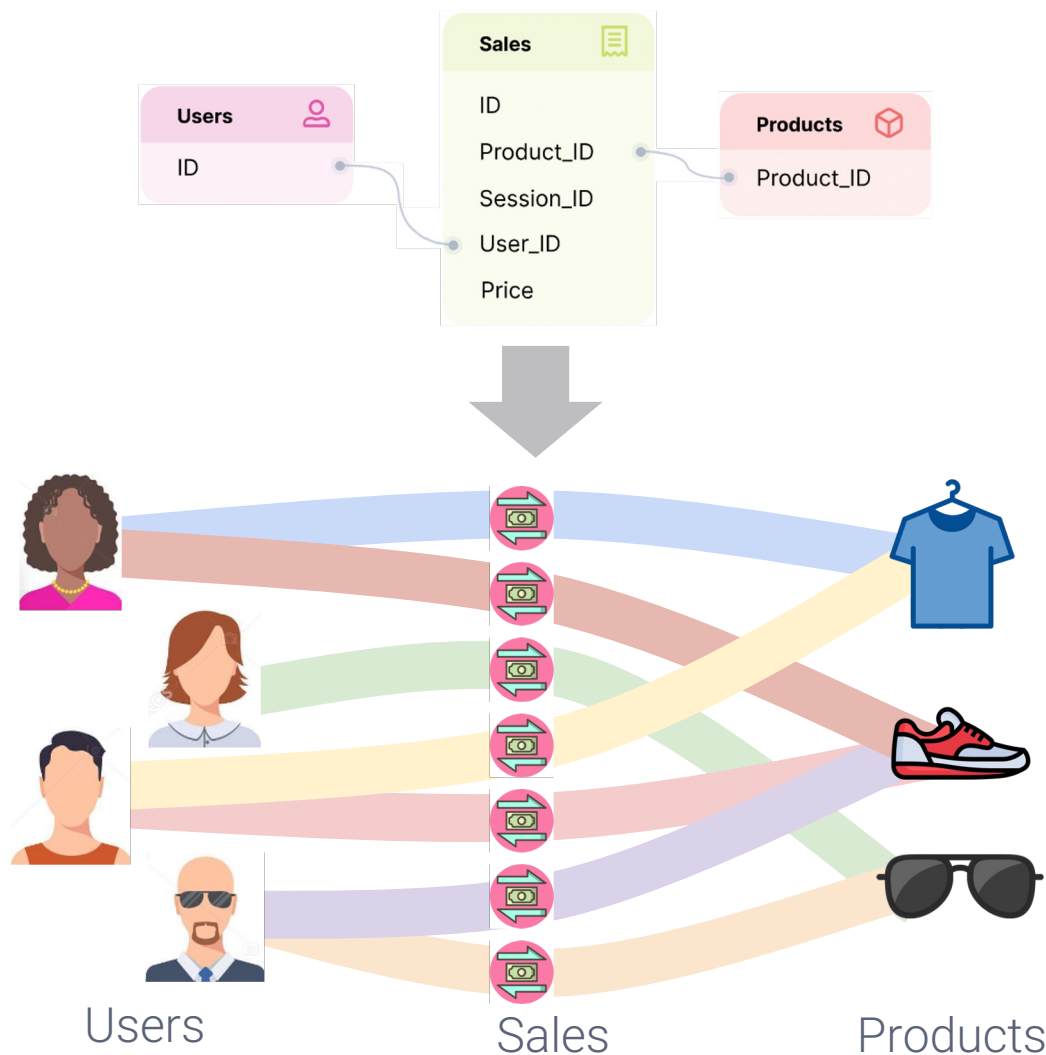


Commerce

Finance

Social Media

Relational Deep Learning



<http://relbench.stanford.edu>

Graphs: Machine Learning

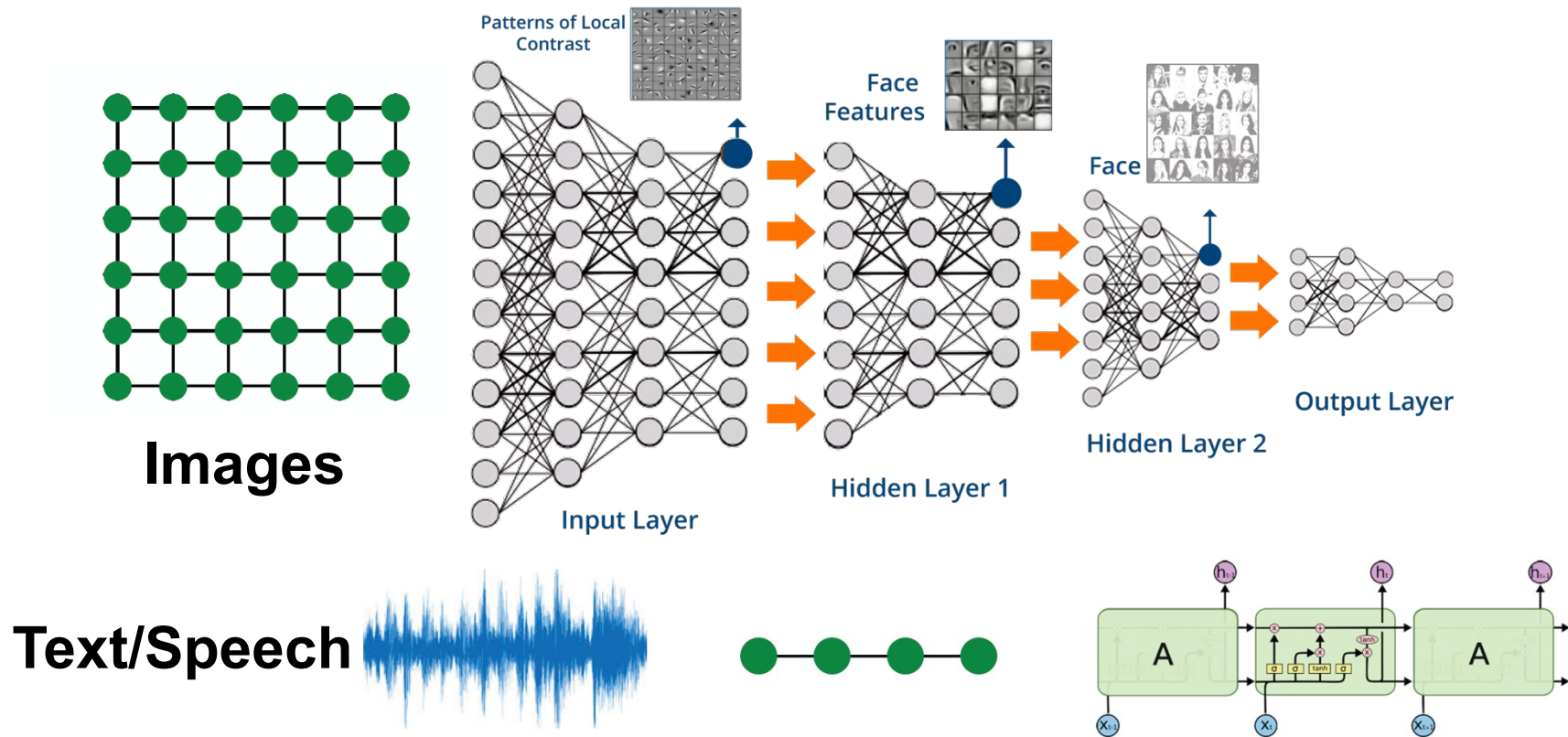
Complex domains have a rich relational structure, which can be represented as a **relational graph**

By explicitly modeling relationships we achieve better performance!

Main question:

How do we take advantage of relational structure for better prediction?

Today: Modern ML Toolbox



Modern deep learning toolbox is designed for simple sequences & grids

Doubt thou the stars are fire,
Doubt that the sun doth move,
Doubt truth to be a liar,
But never doubt I love...

Text



Audio signals



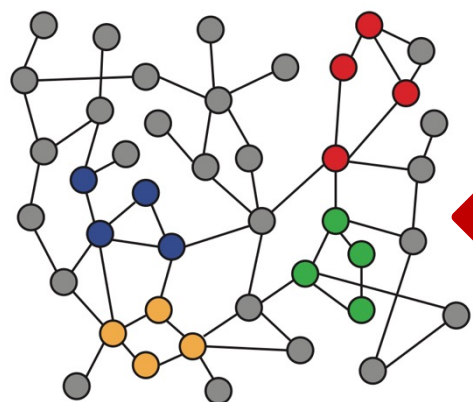
Images

Modern
deep learning toolbox
is designed for
sequences & grids

Why is Graph Deep Learning Hard?

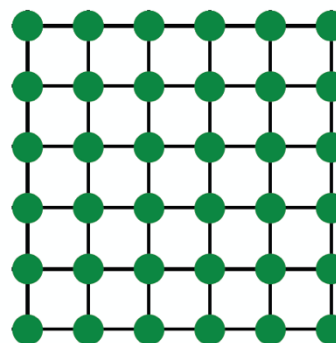
Networks are complex.

- Arbitrary size and complex topological structure (*i.e.*, no spatial locality like grids)

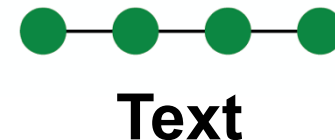


Networks

VS.



Images



Text

- No fixed node ordering or reference point
- Often dynamic and have multimodal features

This Course: CS224W

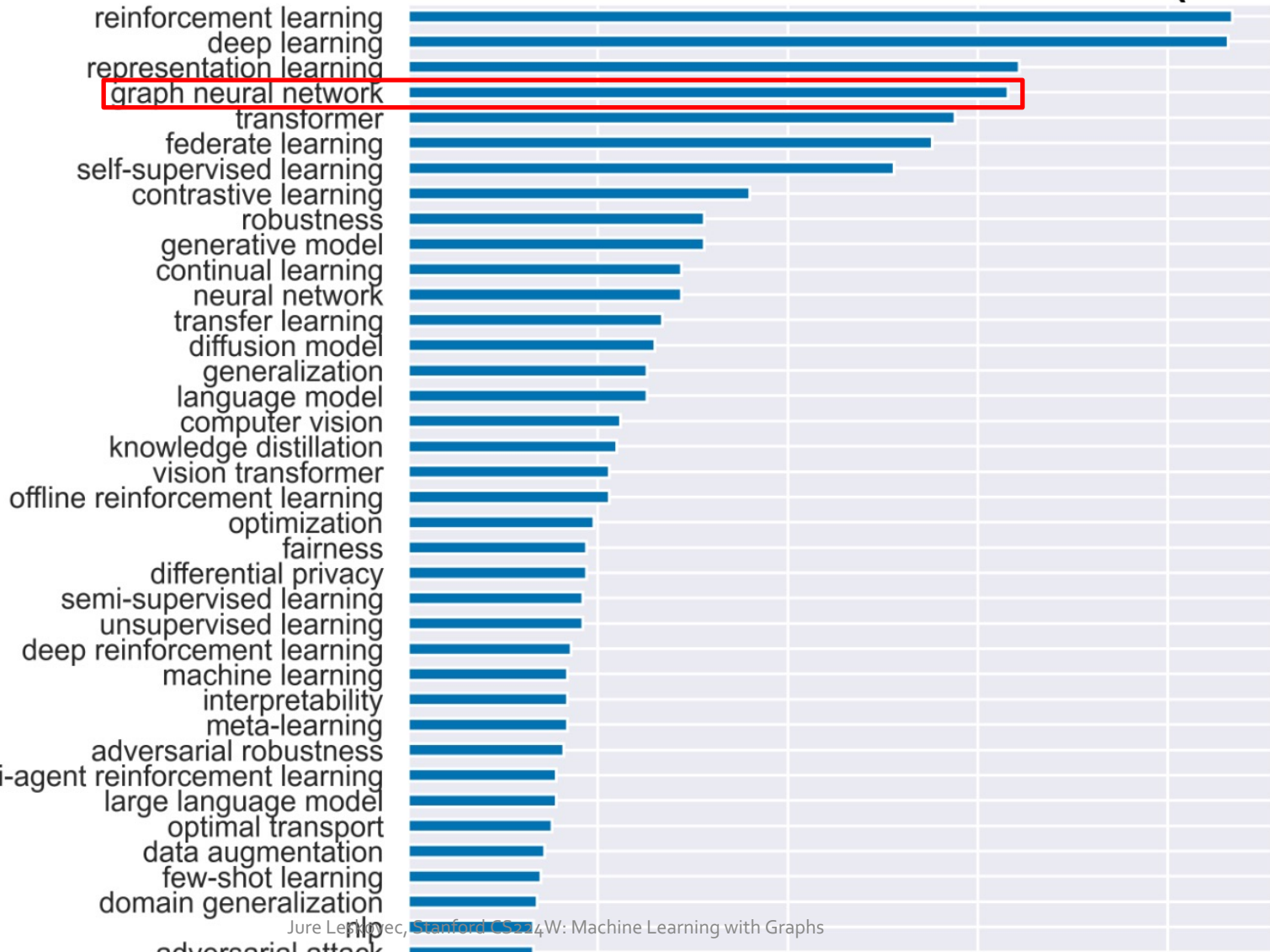
How can we develop neural networks
that are much more broadly
applicable?

Graphs are the new frontier
of deep learning

Hot subfield in ML

50 MOST APPEARED KEYWORDS (2023)

ICLR 2023 keywords

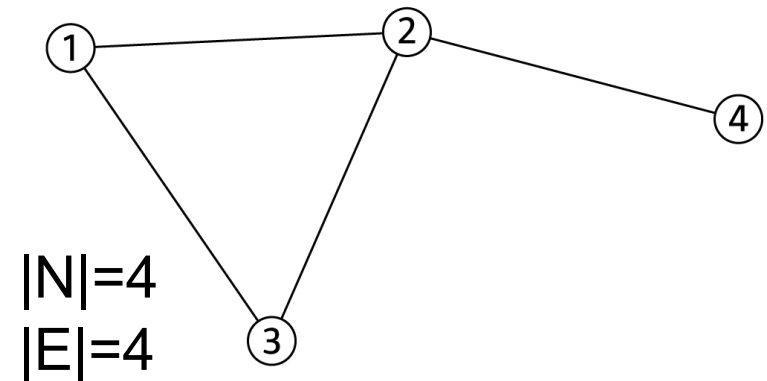
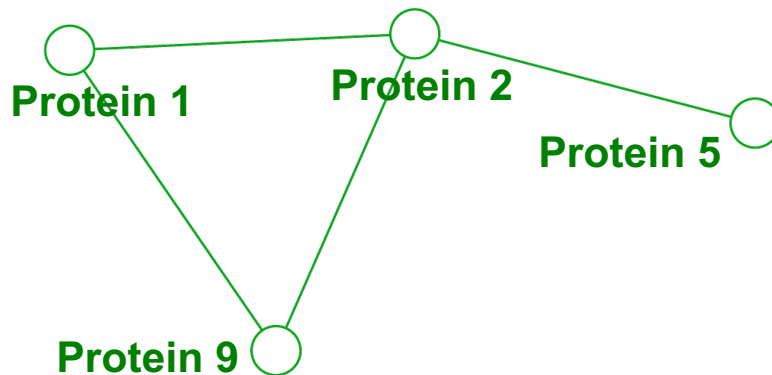
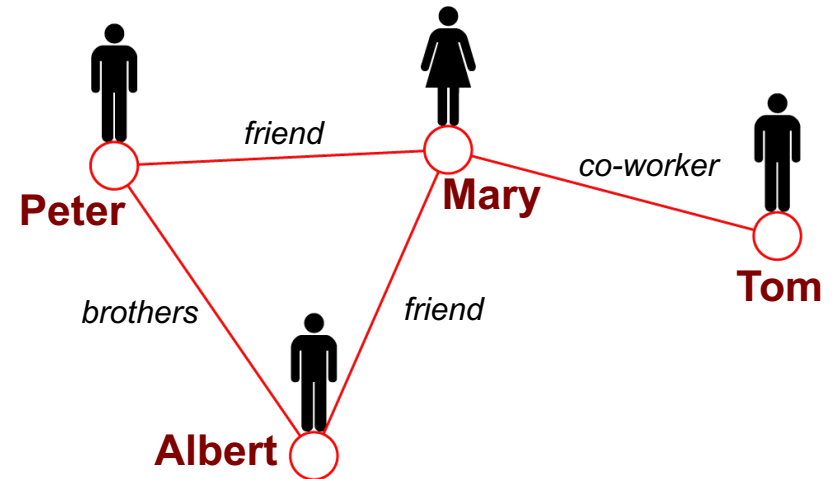
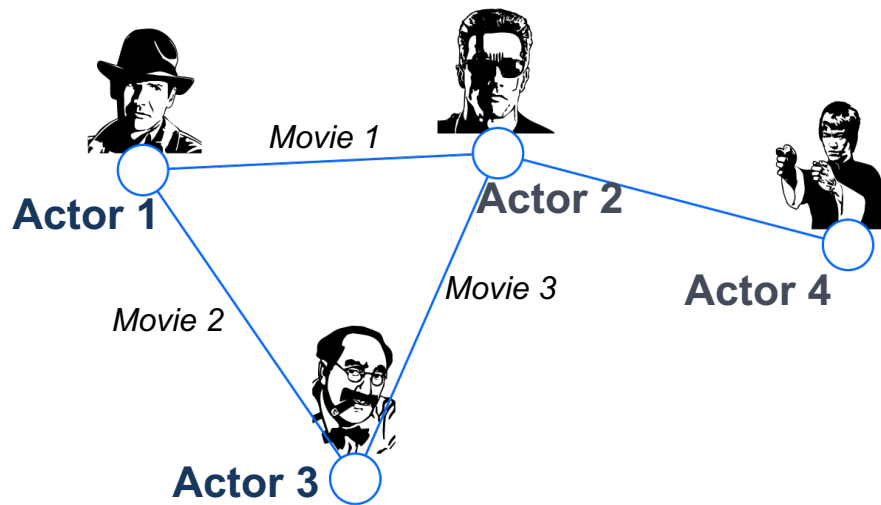


Stanford CS224W: Choice of Graph Representation

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Graphs: A Common Language



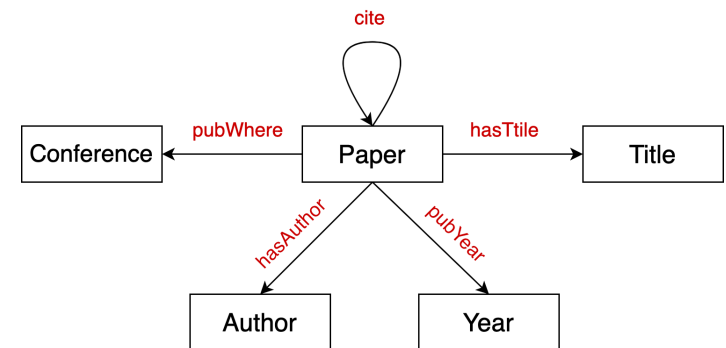
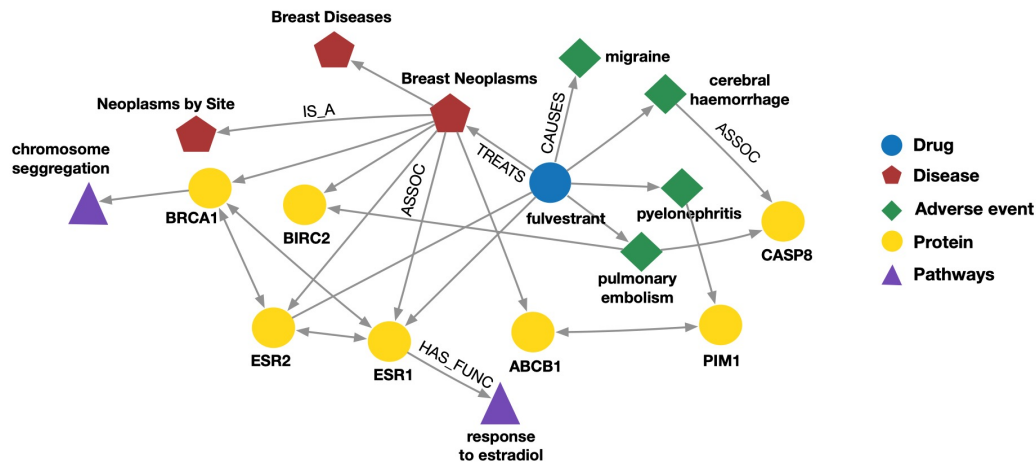
Heterogeneous Graphs

- A heterogeneous graph is defined as

$$G = (V, E, R, T)$$

- Nodes with node types $v_i \in V$
- Edges with relation types $(v_i, r, v_j) \in E$
- Node type $T(v_i)$
- Relation type $r \in R$
- Nodes and edges have **attributes/features**

Many Graphs are Heterogeneous



Biomedical Knowledge Graphs

Example node: Migraine

Example edge: (fulvestrant, Treats, Breast Neoplasms)

Example node type: Protein

Example edge type (relation): Causes

Academic Graphs

Example node: ICML

Example edge: (GraphSAGE, NeurIPS)

Example node type: Author

Example edge type (relation): pubYear

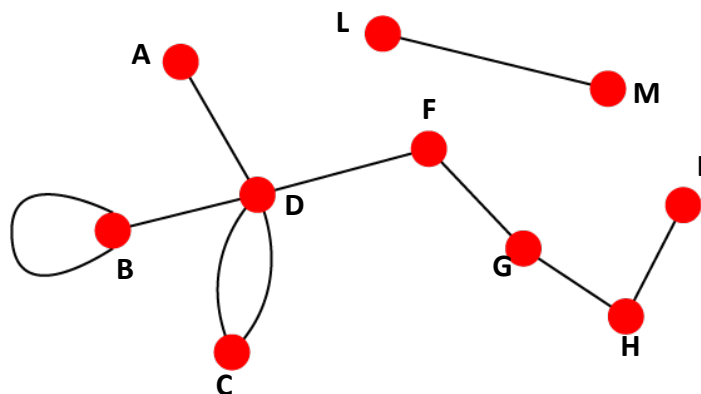
Choosing a Proper Representation

- **How to build a graph:**
 - What are nodes?
 - What are edges?
- **Choice of the proper network representation of a given domain/problem determines our ability to use networks successfully:**
 - In some cases, there is a unique, unambiguous representation
 - In other cases, the representation is by no means unique
 - The way you assign links will determine the nature of the question you can study

Directed vs. Undirected Graphs

Undirected

- **Links:** undirected (symmetrical, reciprocal)

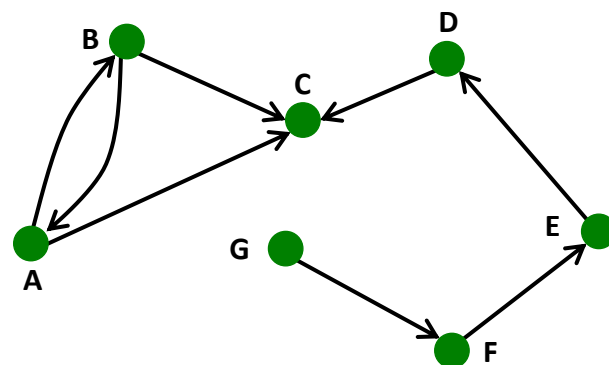


- **Other considerations:**

- Weights
- Properties

Directed

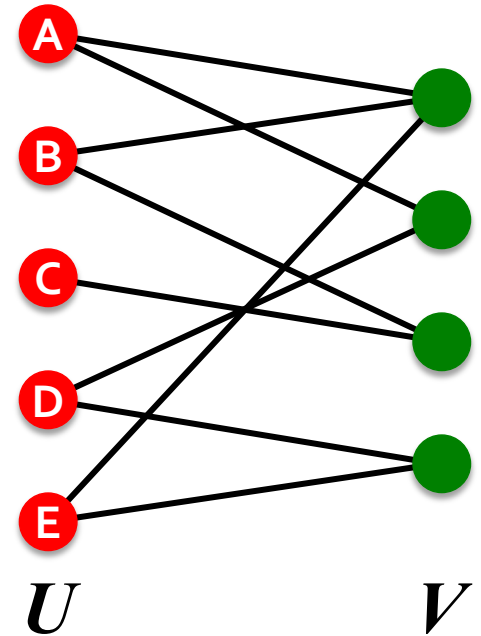
- **Links:** directed



- Types
- Attributes

Bipartite Graph

- **Bipartite graph** is a graph whose nodes can be divided into two disjoint sets U and V such that every link connects a node in U to one in V ; that is, U and V are **independent sets**
- **Examples:**
 - Authors-to-Papers (they authored)
 - Actors-to-Movies (they appeared in)
 - Users-to-Movies (they rated)
 - Recipes-to-Ingredients (they contain)
- **“Folded” networks:**
 - Author collaboration networks
 - Movie co-rating networks

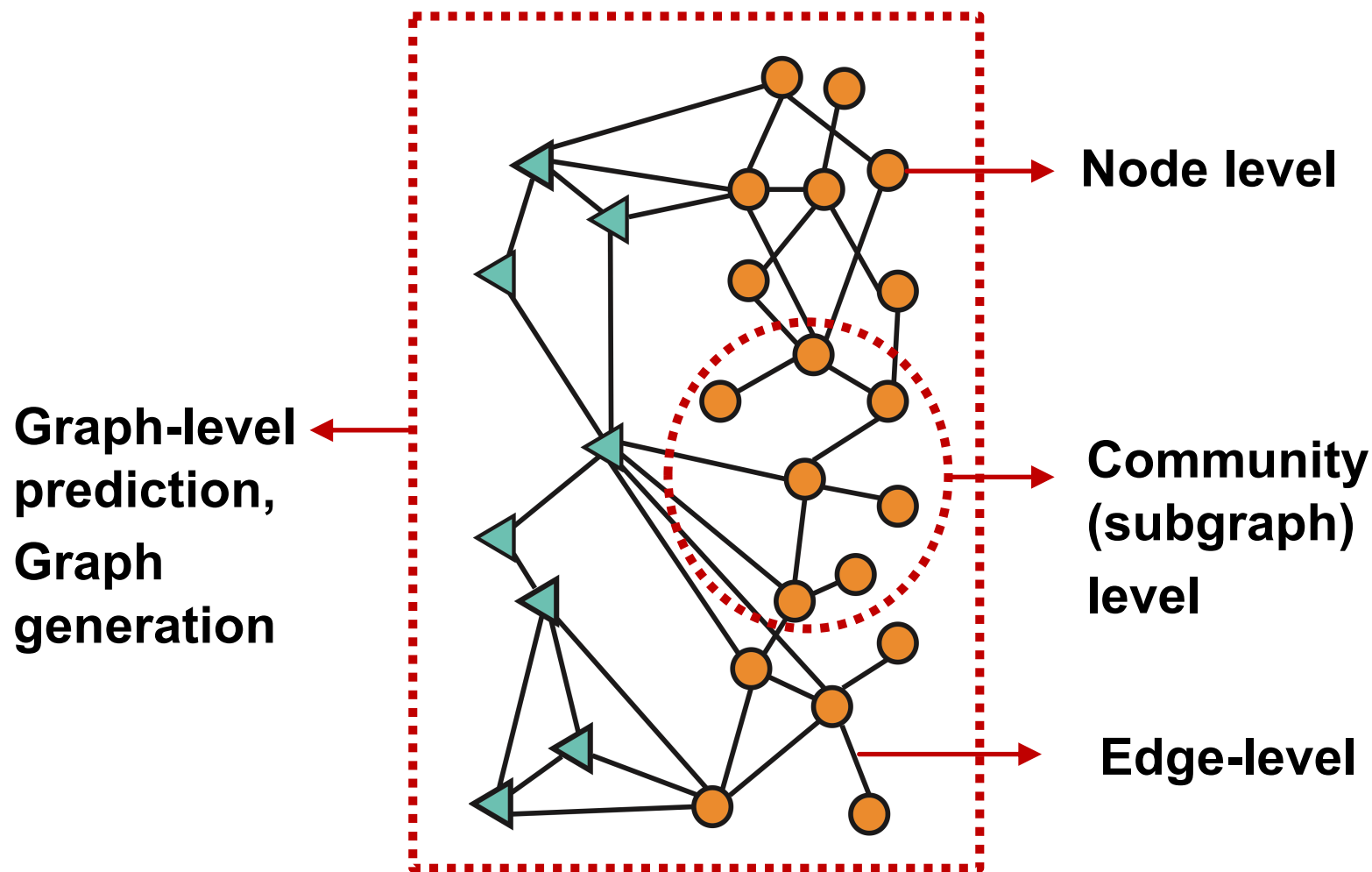


Stanford CS224W: Applications of Graph ML

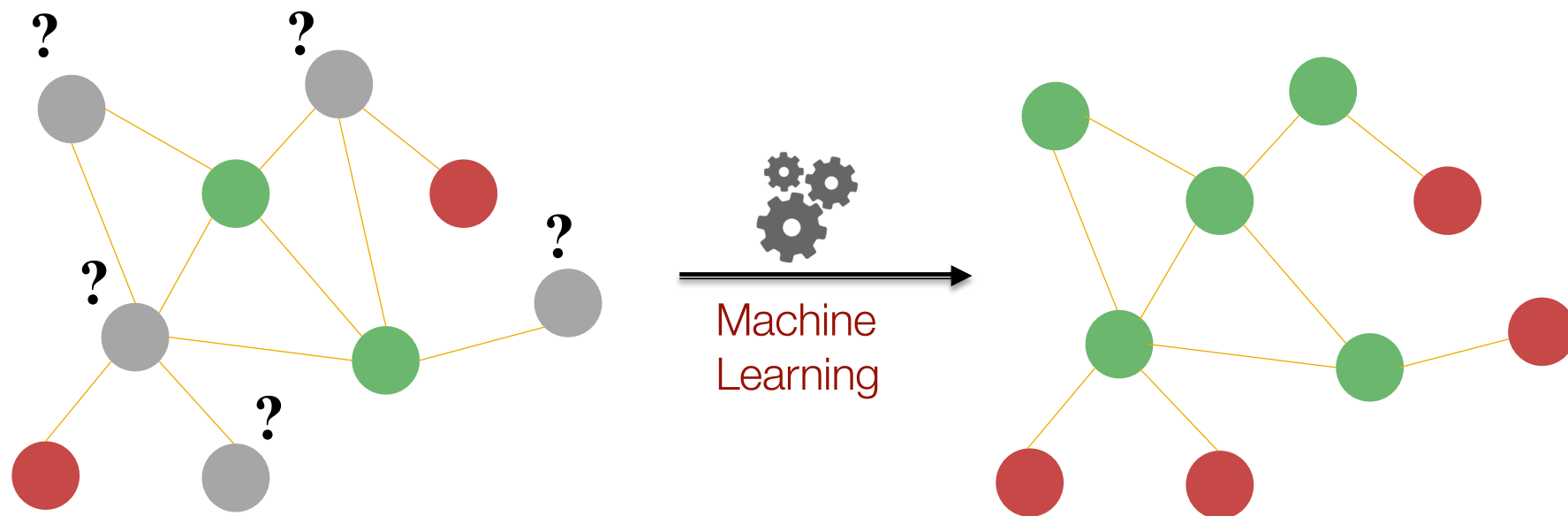
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Different Types of Tasks



Node-Level Tasks

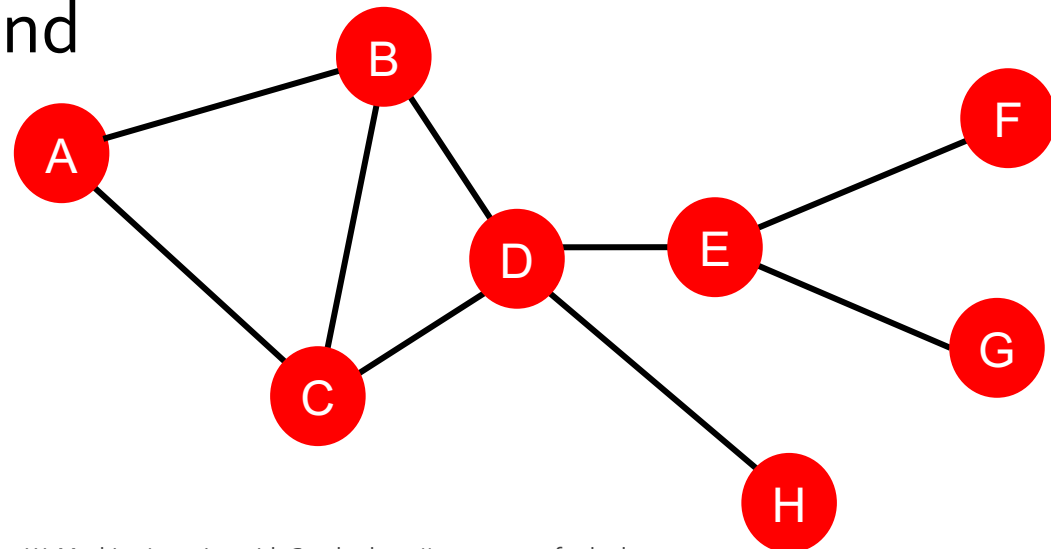


Node classification

Node-Level Network Structure

Goal: Characterize the structure and position of a node in the network:

- Node degree
- Node importance & position
 - E.g., Number of shortest paths passing through a node
 - E.g., Avg. shortest path length to other nodes
- Substructures around the node

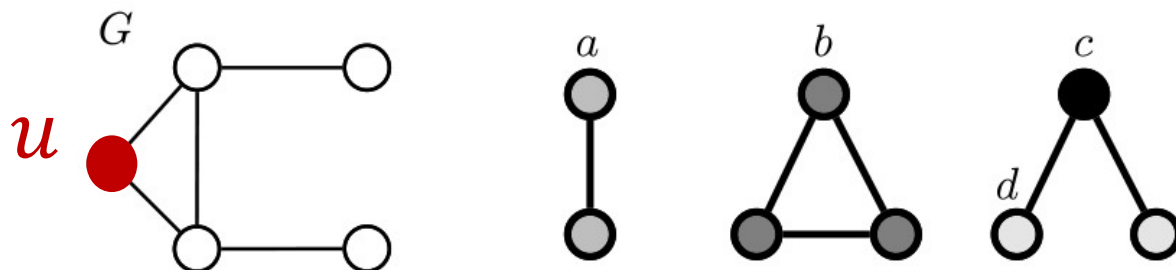


Node's Subgraphs: Graphlets

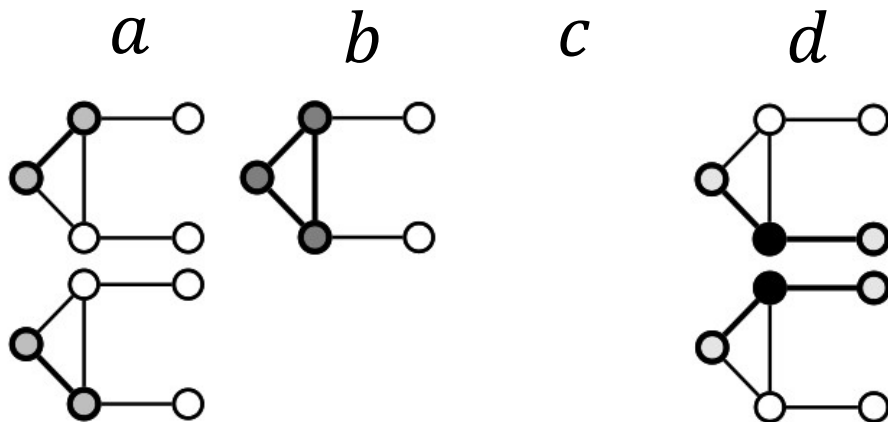
- **Graphlets:** A count vector of rooted subgraphs at a given node.

- **Example:**

All possible graphlets on up to 3 nodes



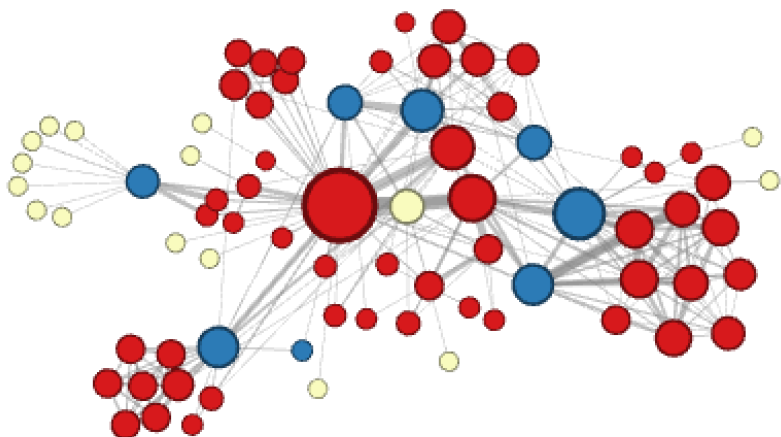
Graphlet instances of node u :



Graphlets of node u :
 a, b, c, d
 $[2, 1, 0, 2]$

Discussion

Different ways to label nodes of the network:



Node features defined so far would allow to distinguish nodes in the above example



However, the features defines so far would not allow for distinguishing the above node labelling

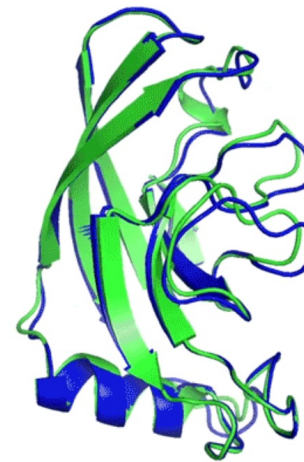
Example (1): Protein Folding

Computationally predict a protein's 3D structure based solely on its amino acid sequence:

For each node predict its 3D coordinates



T1037 / 6vr4
90.7 GDT
(RNA polymerase domain)



T1049 / 6y4f
93.3 GDT
(adhesin tip)

- Experimental result
- Computational prediction

Image credit: [DeepMind](#)

AlphaFold: Impact

Median Free-Modelling Accuracy

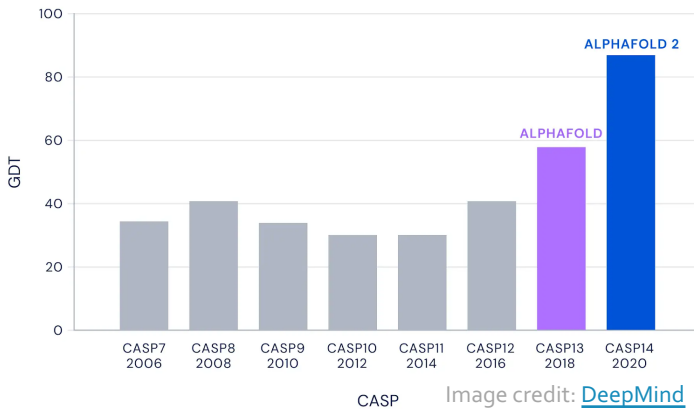


Image credit: [SingularityHub](#)

AlphaFold's AI could change the world of biological science as we know it

DeepMind's latest AI breakthrough can accurately predict the way proteins fold

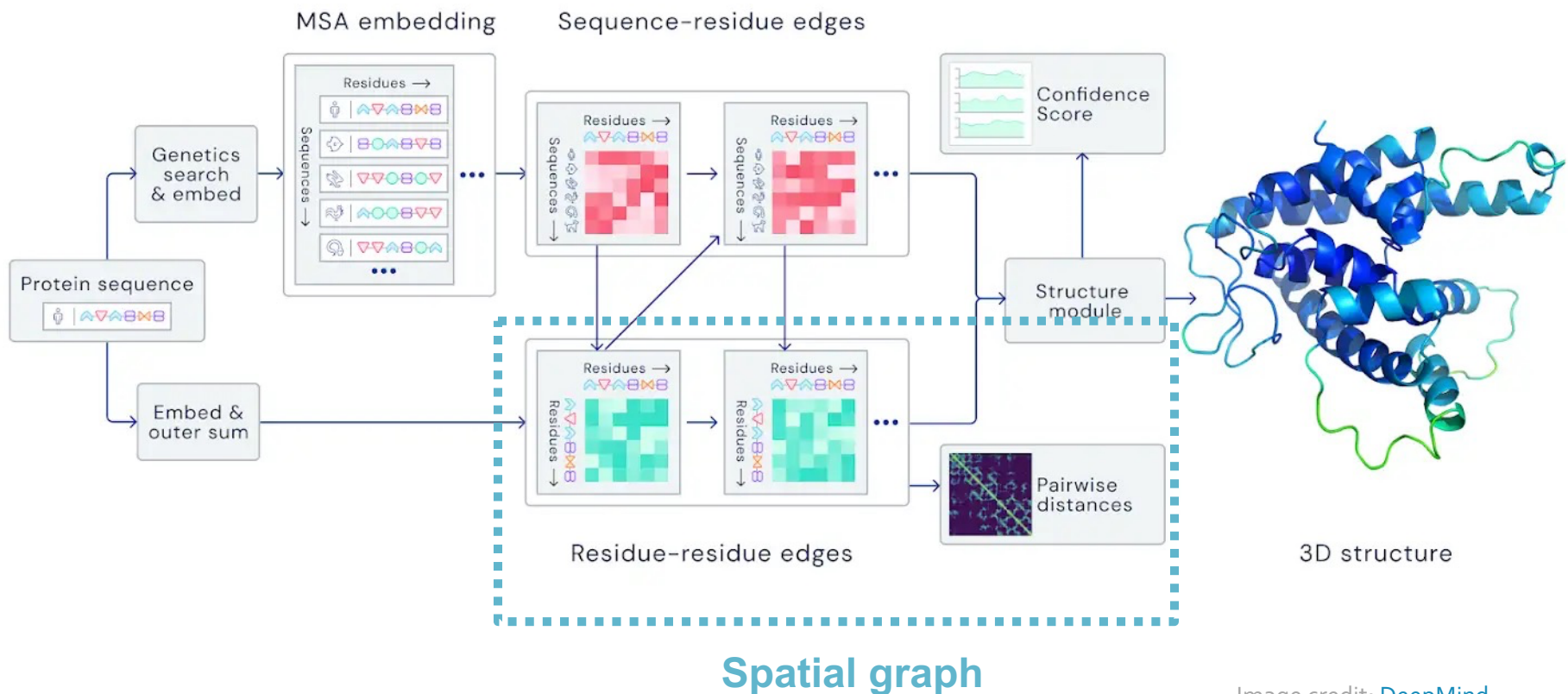
Has Artificial Intelligence 'Solved' Biology's Protein-Folding Problem?

12-14-20

DeepMind's latest AI breakthrough could turbocharge drug discovery

AlphaFold: Solving Protein Folding

- **Key idea:** “Spatial graph”
 - **Nodes:** Amino acids in a protein sequence
 - **Edges:** Proximity between amino acids (residues)



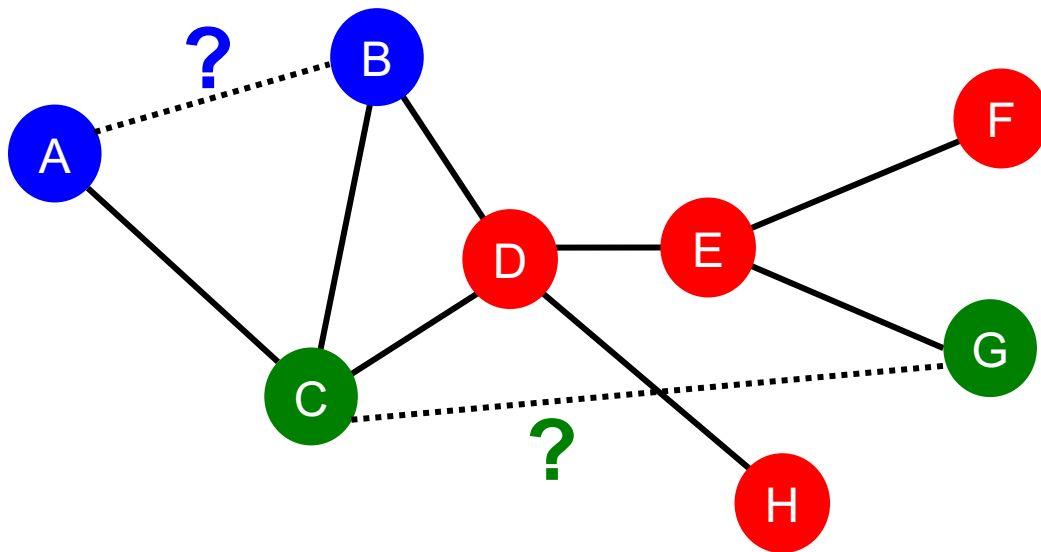
Stanford CS224W: Link Prediction

CS224W: Machine Learning with Graphs
Jure Leskovec, Stanford University
<http://cs224w.stanford.edu>



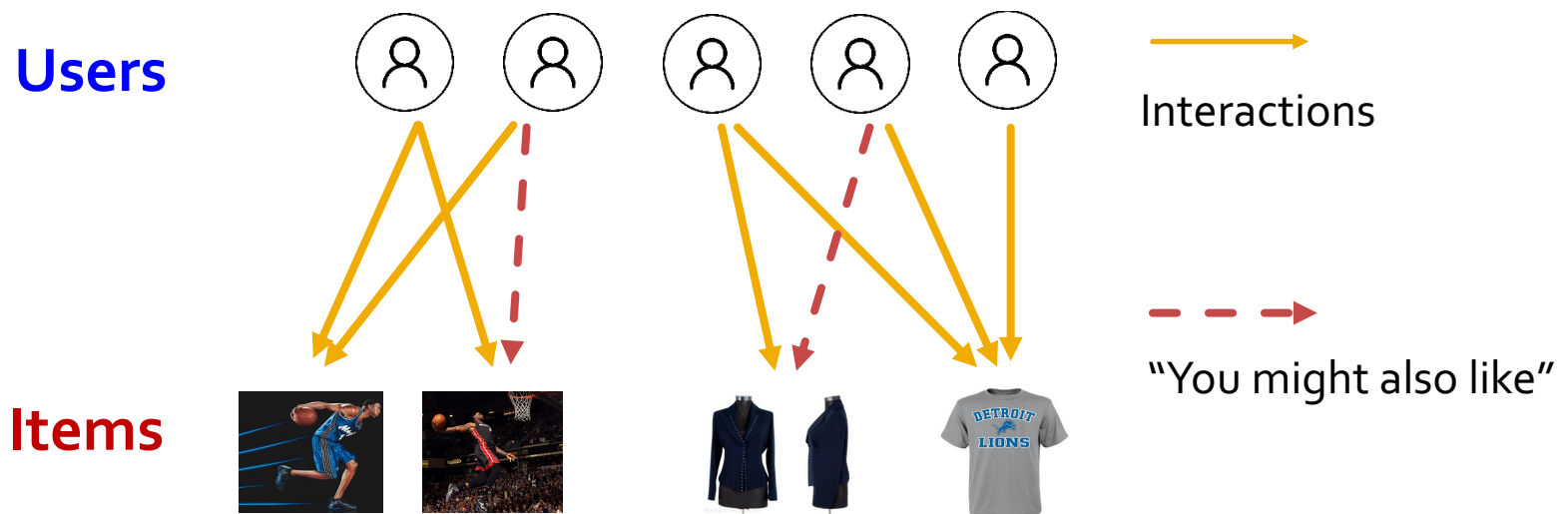
Link-Level Prediction Task

- The task is to predict **new/missing/unknown links** based on the existing links.
- At test time, node pairs (with no existing links) are ranked, and top K node pairs are predicted.
- Task: Make a prediction for a pair of nodes.



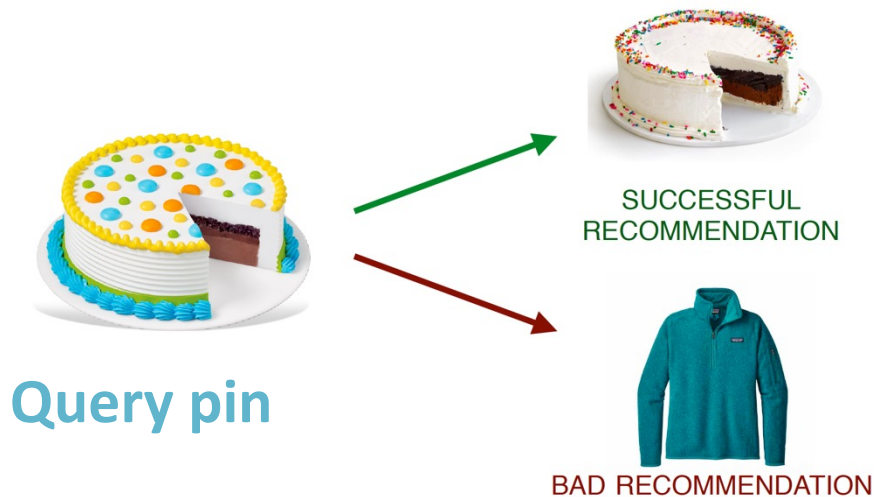
Example (1): Recommender Systems

- **Users interacts with items**
 - Watch movies, buy merchandise, listen to music
 - **Nodes:** Users and items
 - **Edges:** User-item interactions
- **Goal: Recommend items users might like**



PinSage: Graph-based Recommender

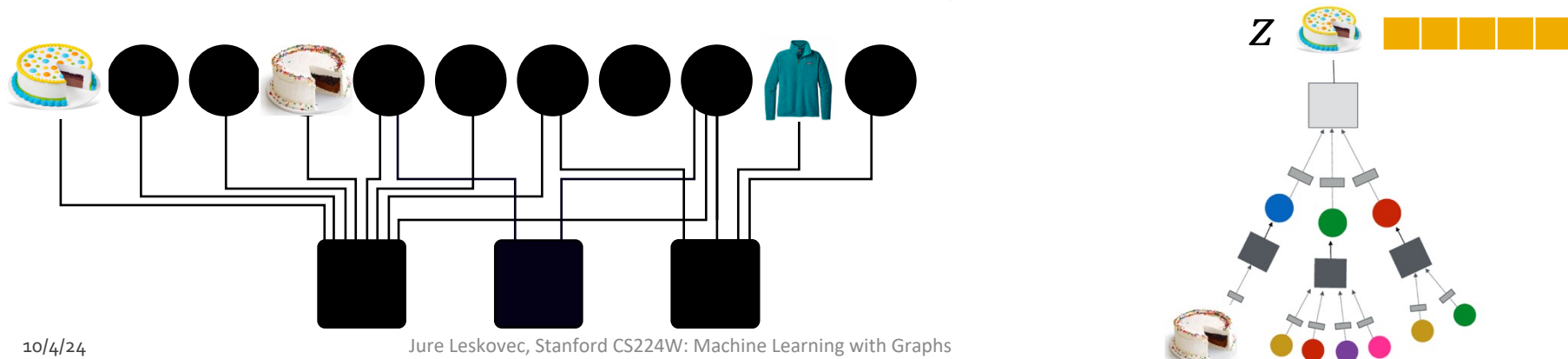
Task: Recommend related pins to users



Task: Learn node embeddings z_i such that

$$d(z_{cake1}, z_{cake2}) < d(z_{cake1}, z_{sweater})$$

Predict whether two nodes in a graph are related



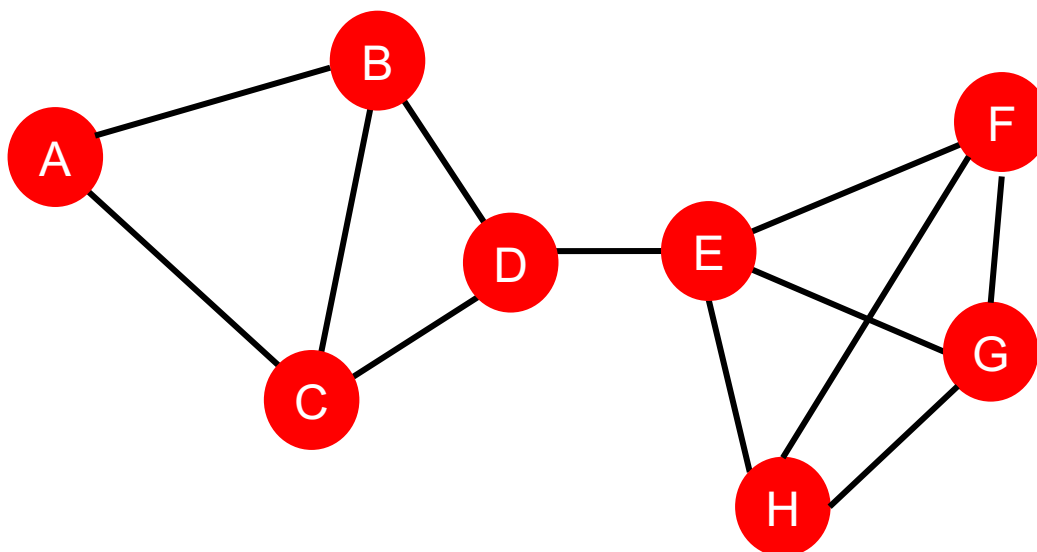
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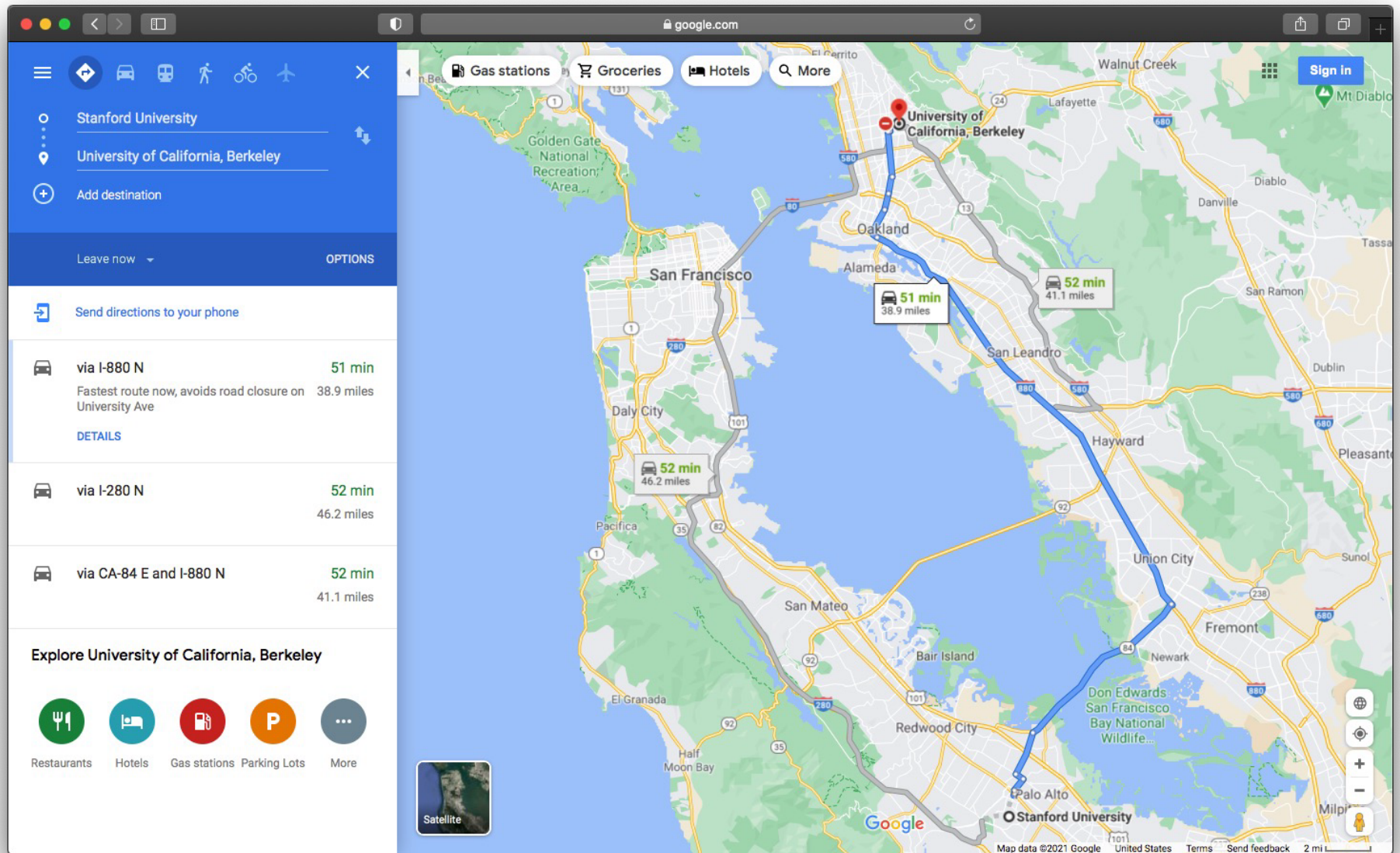


Graph-Level Prediction

- **Goal:** We want make a prediction for an entire graph or a subgraph of the graph.
- **For example:**



Example (1): Traffic Prediction



Road Network as a Graph

- **Nodes:** Road segments
- **Edges:** Connectivity between road segments
- **Prediction:** Time of Arrival (ETA)

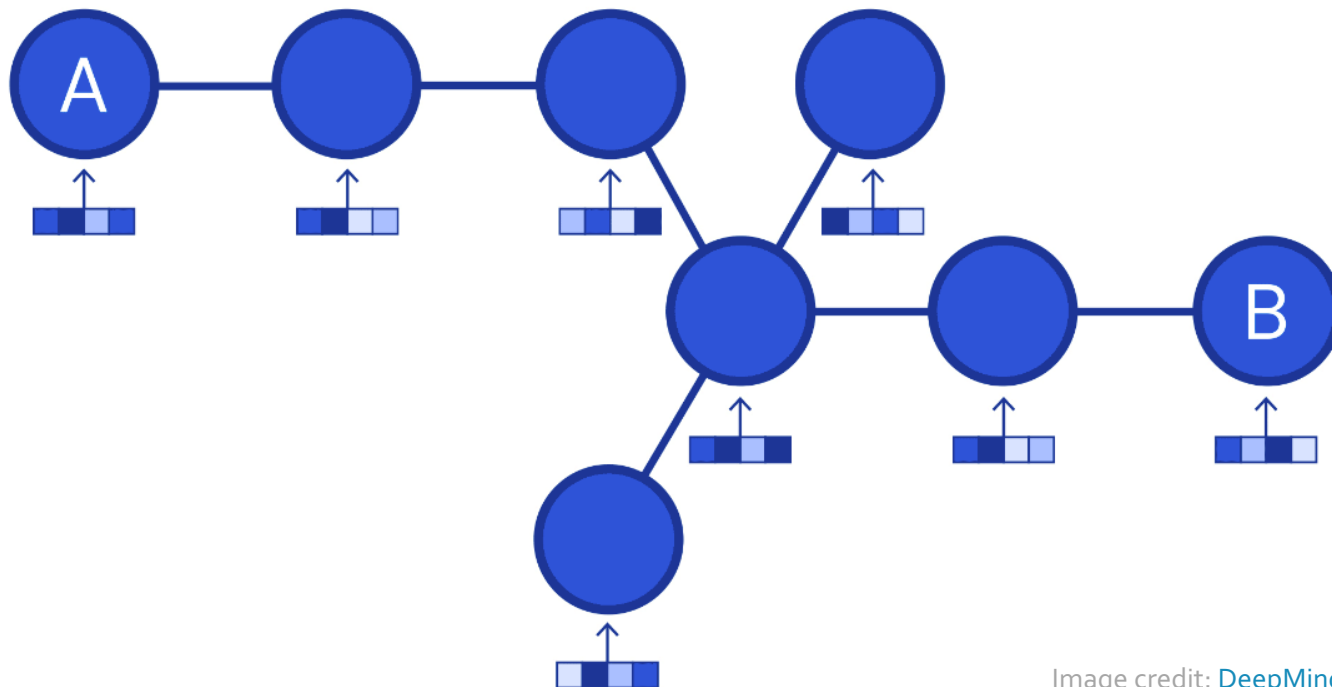
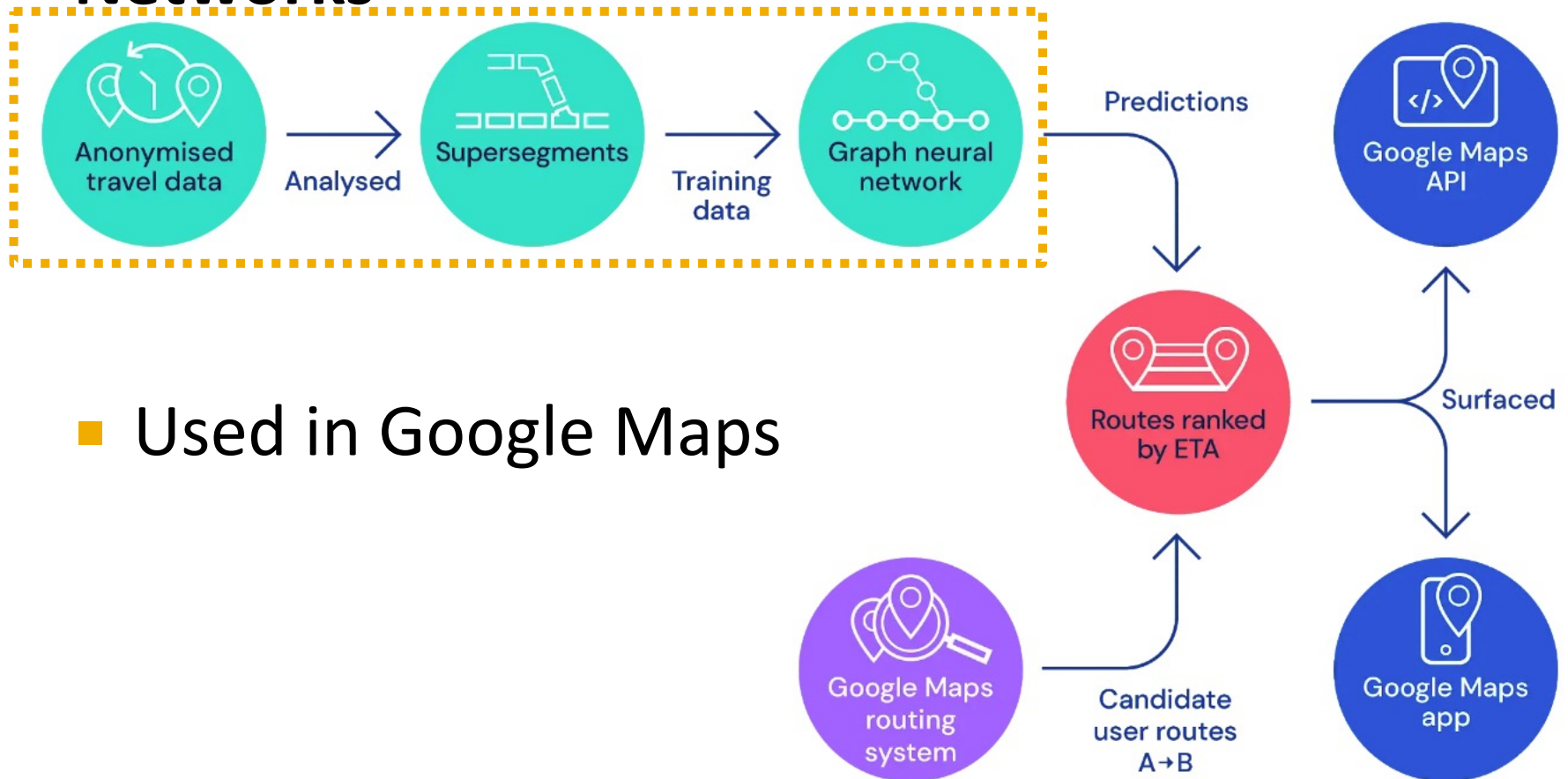


Image credit: [DeepMind](#)

Traffic Prediction via GNN

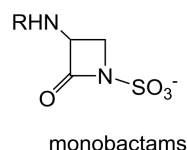
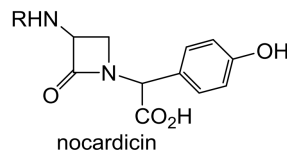
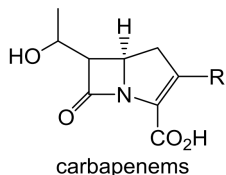
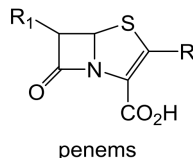
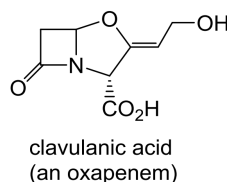
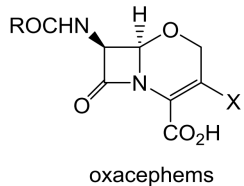
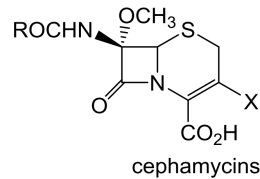
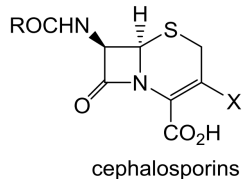
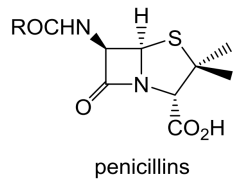
Predicting Time of Arrival with Graph Neural Networks



- Used in Google Maps

Example (2): Drug Discovery

- Antibiotics are small molecular graphs
 - **Nodes:** Atoms
 - **Edges:** Chemical bonds

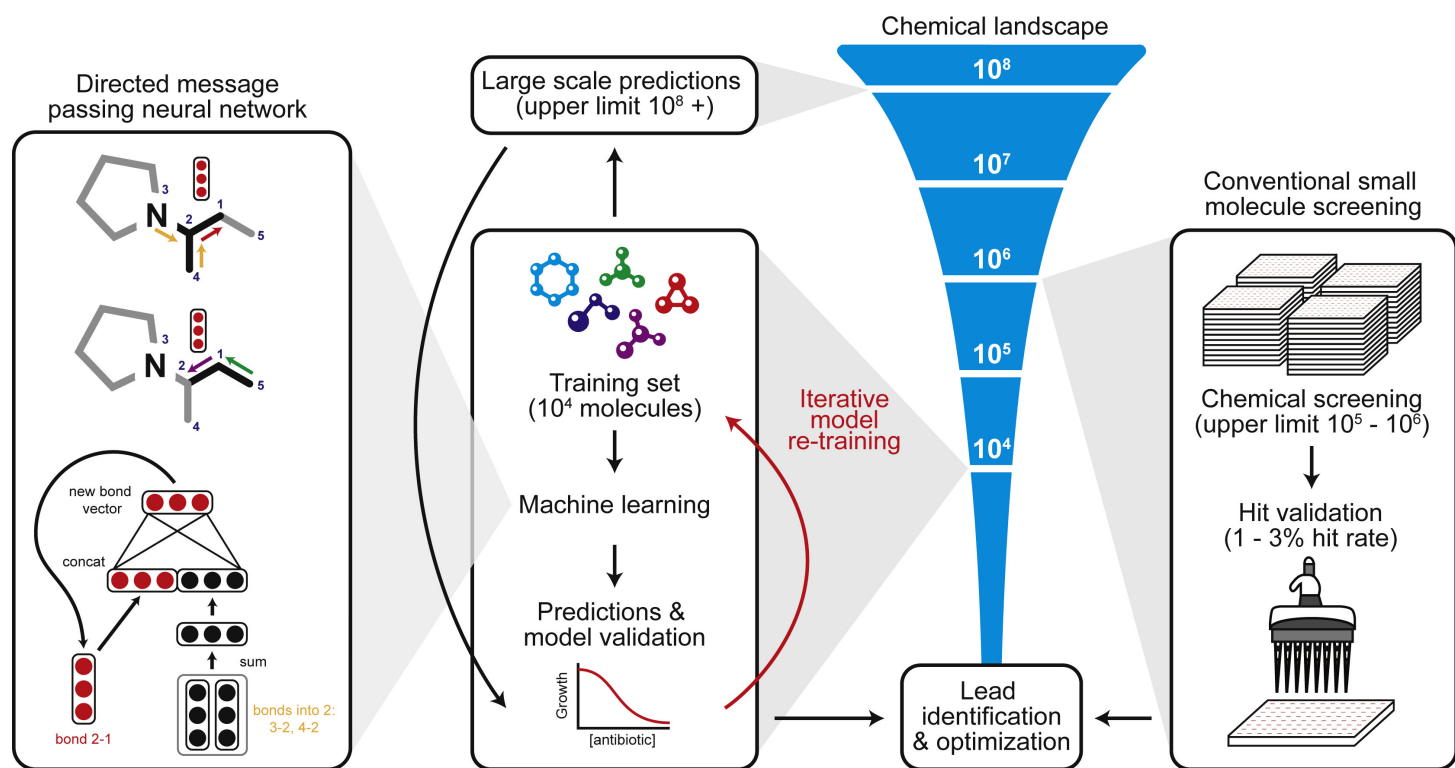


Konaklieva, Monika I. "Molecular targets of β -lactam-based antimicrobials: beyond the usual suspects." *Antibiotics* 3.2 (2014): 128-142.

Image credit: [CNN](#)

Deep Learning for Antibiotic Discovery

- A Graph Neural Network **graph classification model**
- Predict promising molecules from a pool of candidates



Stokes, Jonathan M., et al. "A deep learning approach to antibiotic discovery." *Cell* 180.4 (2020): 688-702.

Summary

ML in the language of graphs:

- **Node-level:**

- Churn
- Life-time value
- Next best action

- **Link-level:**

- Product affinity
- Recommendations

- **Graph-level:**

- Fraud, money laundering

